G-1/173/22

Roll No.

I Semester Examination, January 2022

M.Sc.

INFORMATION TECHNOLOGY

Paper III

(Mathematical Foundations of Computer Science)

Time: 3 Hours] [Max. Marks: 100

Note: All questions are compulsory. Question Paper comprises of 3 Sections. Section A is objective type/multiple choice questions with no internal choice. Section B is short answer type with internal choice. Section C is long answer type with internal choice.

SECTIONA

 $1 \times 10 = 10$

(Objective Type/Multiple Choice Questions)

Choose the correct answer:

- 1. If $x \in \mathbb{N}$ and x is prime, then x is set.
 - (a) Infinite set
- (b) Finite set
- (c) Empty set
- (d) Not a set

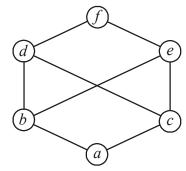
2. Which of the following is De Morgan's law?

(a)
$$P \wedge (Q \vee R) \equiv (P \wedge Q) \vee (P \wedge R)$$

(b)
$$\sim (P \wedge R) \Xi \sim P \vee \sim R, \sim (P \vee R) \Xi \sim P \wedge \sim R$$

(c)
$$P \lor \sim P \Xi$$
 True, $P \land \sim P \Xi$ False

- (d) None of the above
- **3.** $\neg (A \lor q) \land (A \land q)$ is a :
 - (a) Tautology
- (b) Contingency
- (c) Contradiction
- (d) None of the mentioned
- **4.** The graph given below is an example of :



- (a) non-lattice poset (b) bounded lattice
- (c) semilattice
- (d) partial lattice
- **5.** Every poset that is a complete semilattice must always be a :
 - (a) sublattice
- (b) complete lattice
- (c) partial lattice
- (d) free lattice

6. Intersection of subgroups is a :

(a) group

- (b) subgroup
- (c) cyclic group
- (d) semigroup

7. The tree elements are called:

(a) vertices

- (b) nodes
- (c) pointes
- (d) edges

8. In a the vertex set and the edge set are finite sets.

- (a) finite graph
- (b) connected graph
- (c) infinite graph
- (d) bipartite graph

9. Breadth First Search traversal of a binary tree finds its applications :

- (a) Cloud computing
- (b) Weighted graph
- (c) Euler path
- (d) Peer to peer networks

10. For very spanning tree with n vertices and n edges what is the least number of different Spanning trees can be formed?

(a) 2

(b) 3

(c) 4

(d) 5

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P.T.O.

SECTION B

 $6 \times 5 = 30$

(Short Answer Type Questions)

Note: All the five questions are compulsory.

Unit-I

1. Find a set of largest possible size that is a subset of both {1, 2, 3, 4, 5} and {2, 4, 6, 8, 10}.

Or

Let A $\{x \in \mathbb{N} : 4 \le x < 12\}$ and B $\{x \in \mathbb{N} : x \text{ is even}\}$. (a) Find A \cap B. (b) Find A \setminus B.

Unit-II

2. Prove that the statements $\neg (P \rightarrow Q)$ and $P \land \neg Q$ are logically equivalent without using truth tables.

Or

Define Boolean Algebra. Explain Switching Circuits.

Unit-III

3. What are the properties of a Group? Show that the set G = {1} forms a group with respect to multiplication.

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Or

Consider the function $f: \mathbb{Z} \to \mathbb{Z}$ given by :

$$f(n) = \begin{cases} n+1 & \text{if } n \text{ is even} \\ n-3 & \text{if } n \text{ is odd.} \end{cases}$$

- (a) If f injective? Prove your answer
- (b) If f surjective? Prove your answer

Unit-IV

4. Suppose you have a graph with v vertices and e edges that satisfies v = e + 1. Must the graph be a tree? Prove your answer.

Or

Prove Euler's formula using induction on the number of edges in the graph.

Unit-V

5. Explain Binary Tree Traversal with the help of appropriate examples.

Or

Describe different types of trees and write the Properties of Tree.

SECTION C

 $12 \times 5 = 60$

(Long Answer Type Questions)

Note : All the five questions are compulsory.

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Unit-I

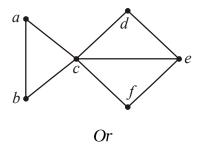
1. What is De Morgan's Law? Describe in detail De Morgan's law Cardinality.

Or

What is recursive function? Explain Algebra of Proposition and propositional Functions.

Unit-II

2. Find all spanning trees of the gaph below. How many different spanning trees are there? How many different spanning trees are there up to isomorphism (that is, if you grouped all the spanning trees by which are isomorphic, how many groups would you have)?



???

Unit-III

3. If R is a ring such that $a^2 = a \forall a \in R$ prove that $a + a = 0 \forall a \in R$. i.e., each element of R is its own additive inverse.

Or

What are Polynomials ? Explain Polynomials Roots and its Applications.

Unit-IV

4. Describe in detail Dijkastra's Algorithm with suitable example.

Or

What is Simple Graph? Explain Graph and its types.

Unit-V

- **5.** How many lattice paths start at (3, 3) and :
 - (a) ends at (10, 10)?
 - (b) end at (10, 10) and pass through (5, 7)?
 - (c) end at (10, 10) and avoid (5, 7)?

Or

Explain, why the coefficient of x^5y^3 the same as the coefficient of x^3y^5 in the expansion of $(x+y)^8$?

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